

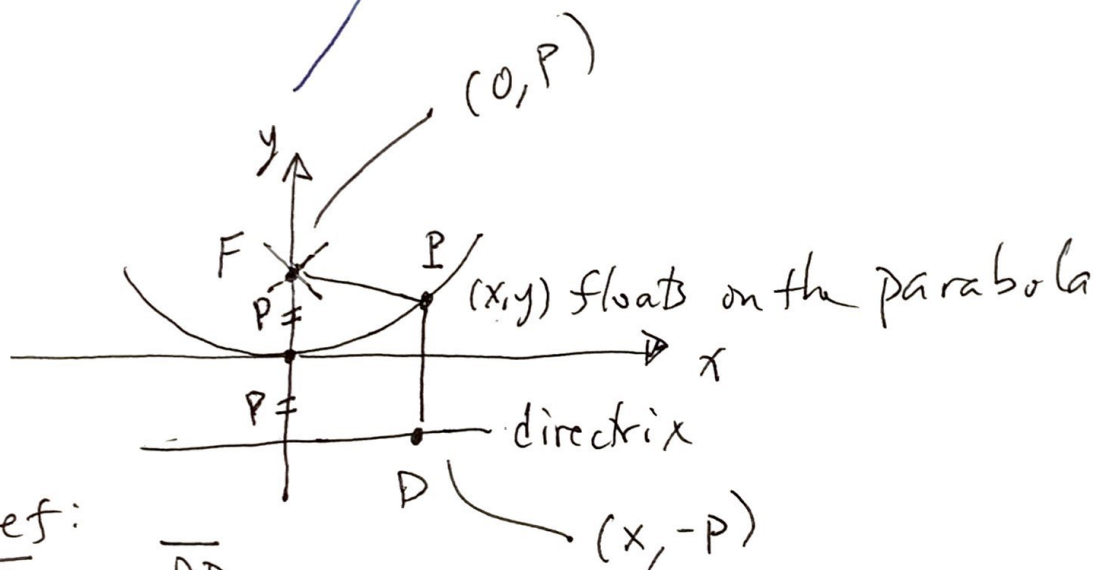
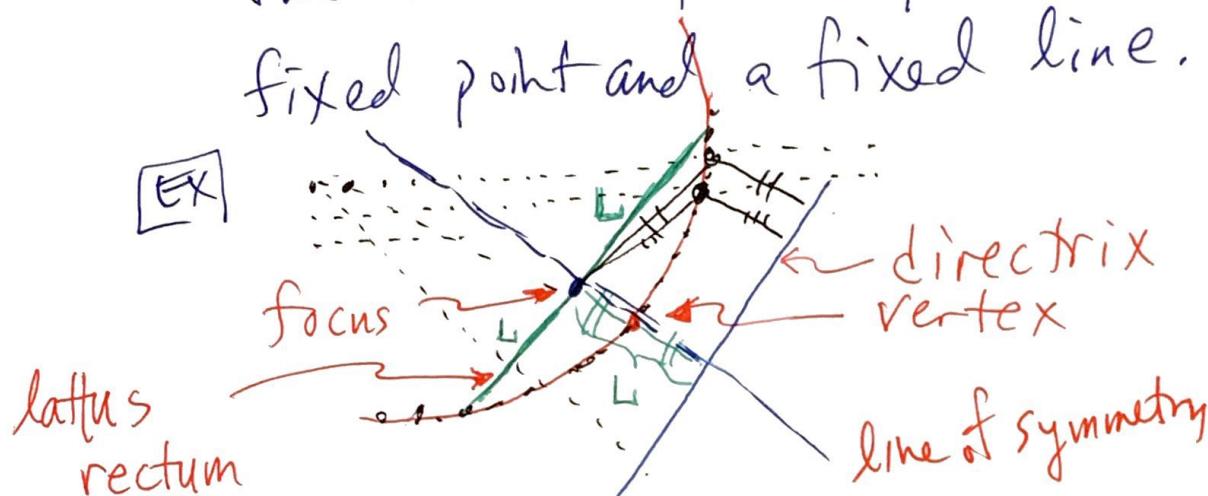
10.3 Parabola

①

Geometric definition of a parabola:

The locus of points equidistant from a fixed point and a fixed line.

[EX]



Geom. Def:

$$m \overline{FP} = m \overline{PD}$$

$$\sqrt{(0-x)^2 + (p-y)^2} = \sqrt{(x-x_0)^2 + (y-(-p))^2}$$

$$x_P = x_D$$

$$x^2 + \cancel{p^2} - 2py + \cancel{y^2} = 0 + \cancel{y^2} + 2yp + \cancel{p^2}$$

$$x^2 = 4py$$

or

$$4py = x^2$$

Alg I: $y = ax^2 + bx + c$

Alg II: $y = a(x-h)^2 + k$

PreCal: $4py = x^2$

$$4p(y-k) = (x-h)^2$$

EX

is $x^2 + 12x - 6y^2 - 51 + 82 = 0$ a parabola?

No does not look like it would factor into

$$4p(y-k) = (x-h)^2 \text{ since we}$$

see a " y^2 " term. This is most likely a hyperbola

EX

Give the vertex, focus, directrix and graph:

(a)

$$y = \frac{1}{8}x^2$$

(i) opens up or sideways?

(ii) form $4py = x^2$

here $8y = x^2$

(iii) match the 8 with $4p$ and solve: $p=2$

(iv) • vertex @ $(x,y) = (0,0)$

• focus @ $(x,y) = (0,2)$

• directrix: $y = -2$

(v) plot the above, plot the
latus rectum end points:

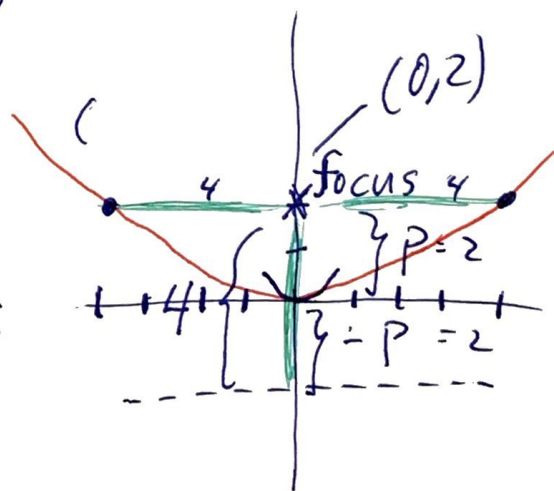
$$(0,2) + (0 \pm 4, 2)$$

$$(-4, 2) \text{ and } (4, 2)$$

$$y = x^2$$

$$x = y^2$$

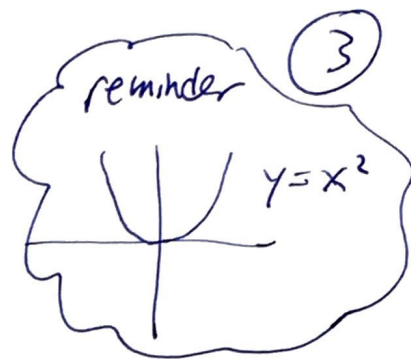
$$x = -y^2$$



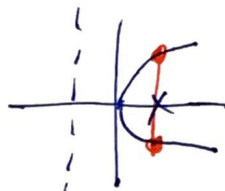
* side way si:

EX

$$x = \frac{y^2}{36}$$



(i) Up/Down or L/R?



(ii) form $4px = y^2$

(iii) match : $36x = y^2$ to $4px = y^2 \Rightarrow p = 9$

(iv) data: vertex : (0,0)

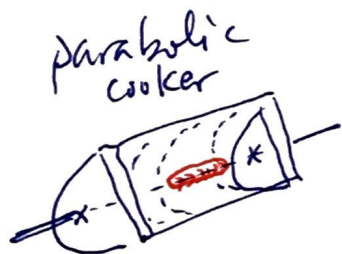
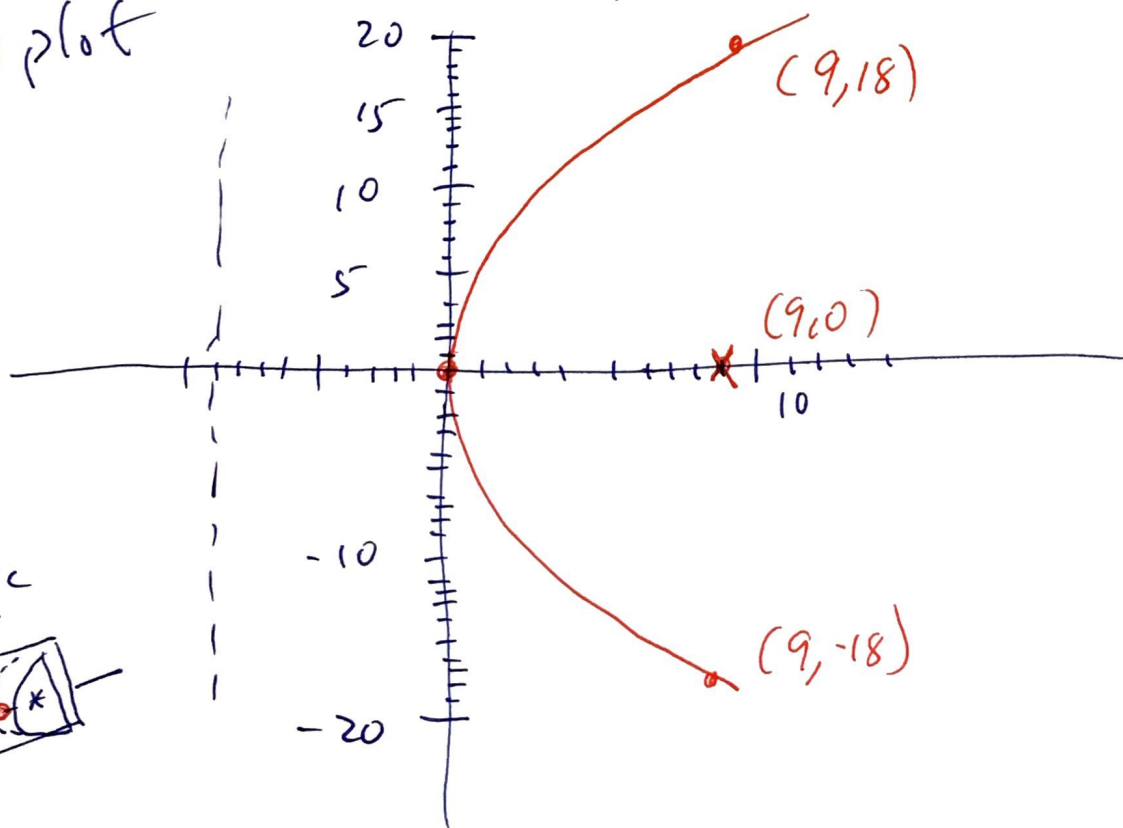
focus : (p, 0) = (9, 0)

directrix: $x = -9$

L.R: (9, +2p) = (9, 18)

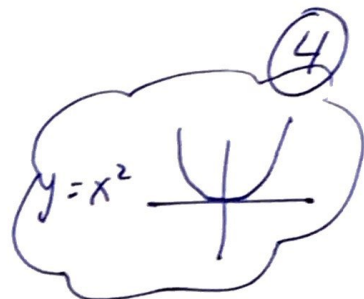
(9, -2p) = (9, -18)

(v) plot



* off origin vertices.

EX ^{Analyze this}
 $(x+4)^2 = 24(y+1)$



(i) L/R or Up/Dn?

(ii) form $4p(y-k) = (x-h)^2$

(iii) match $24(y+1) = (x+4)^2$

$24 = 4p$ and $p = 6$

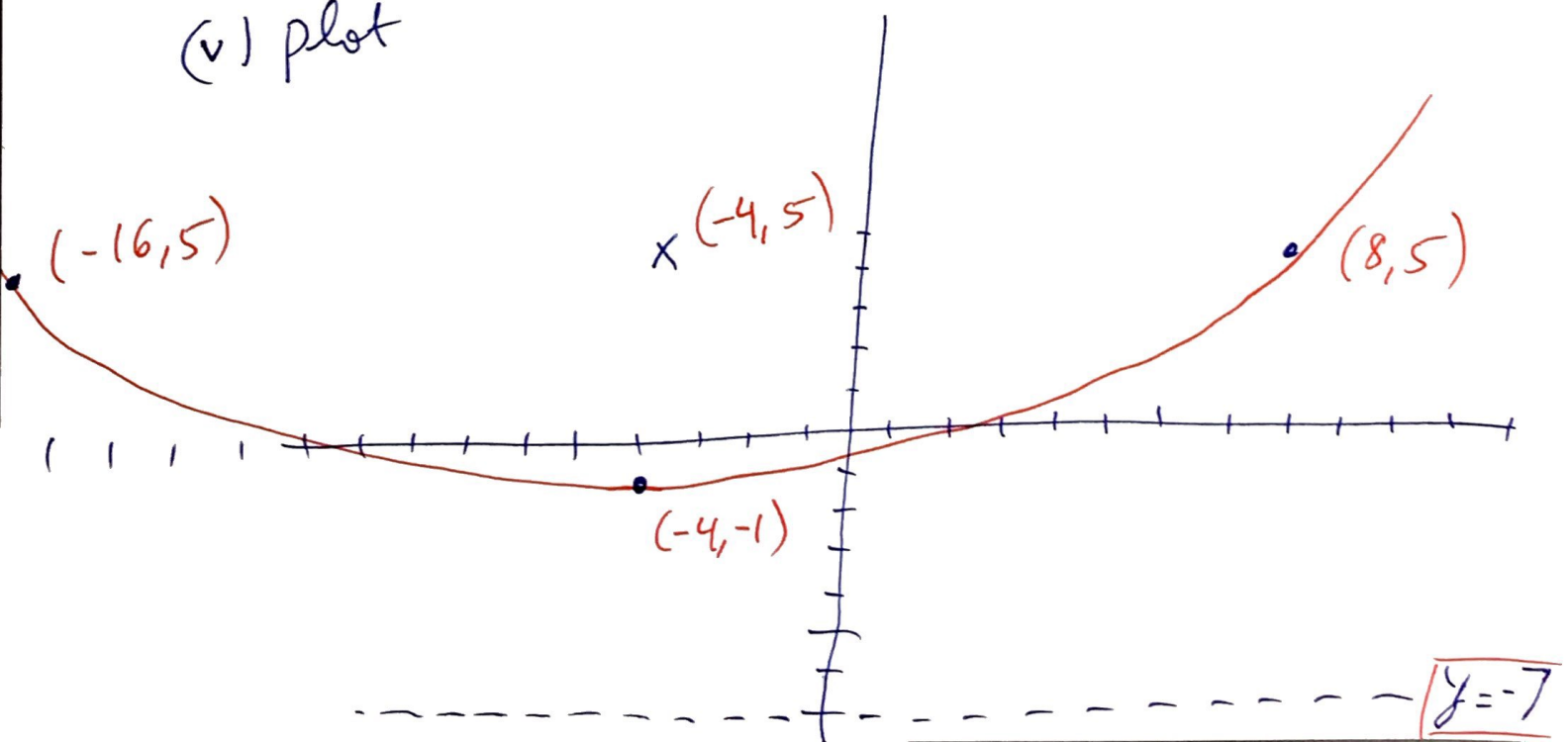
(iv) Data: vertex: $(x, y) = (-4, -1)$ opens up
focus: $(-4, -1) + (0, 6) = (-4, 5)$

directrix: $y = -1 - 6 = -7$ $y = -7$

L.R: $(-4 - 2 \cdot 6, 5) \neq (-4 + 2 \cdot 6, 5)$

$(-16, 5), (8, 5)$

(v) plot



* C.S.I.

(5)

EX describe & give eqn & graph:

vertex is $(-2, 3)$, directrix $x = -\frac{7}{2}$
 and focus is @ $(-\frac{1}{2}, 3)$ *superfluous info.*

plot data given

• vertex & directrix tells us we open right

• form:

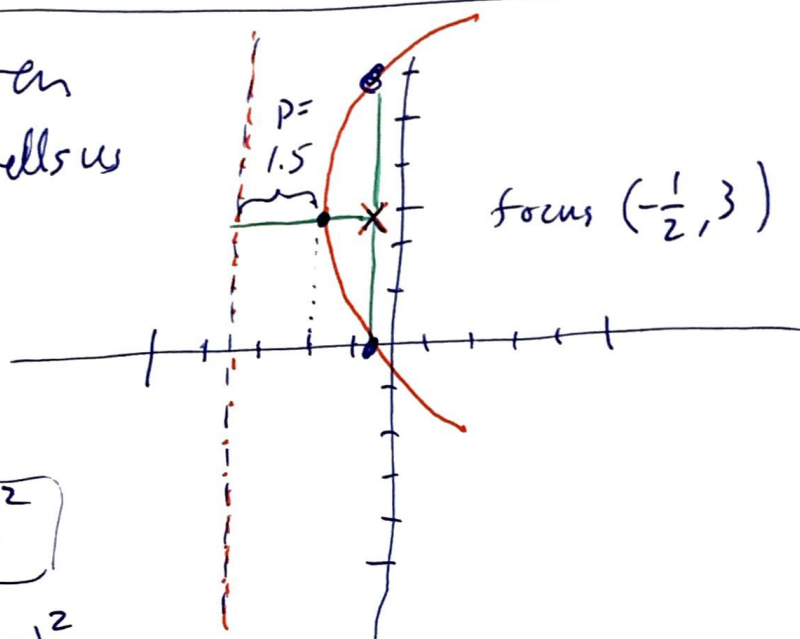
$$4px = y^2$$

$$4p(x-h) = (y-k)^2$$

$$4\left(\frac{3}{2}\right)(x+2) = (y-3)^2$$

• eqn $6(x+2) = (y-3)^2$

• L.R: $\begin{cases} (-\frac{1}{2}, 3+2p) = (-\frac{1}{2}, 6) \\ (-\frac{1}{2}, 3-2p) = (-\frac{1}{2}, 0) \end{cases}$



[2] Find the vertex, focus, directrix eqn, latus rectum endpoints, then graph:

$$y = x^2$$

(i) up/down or left/right?

(ii) $4py = x^2$

(iii) match to $y = x^2$ so $4p = 1$, $p = \frac{1}{4}$

(iv) data: vertex @ $(0, 0)$
focus @ $(0, \frac{1}{4})$

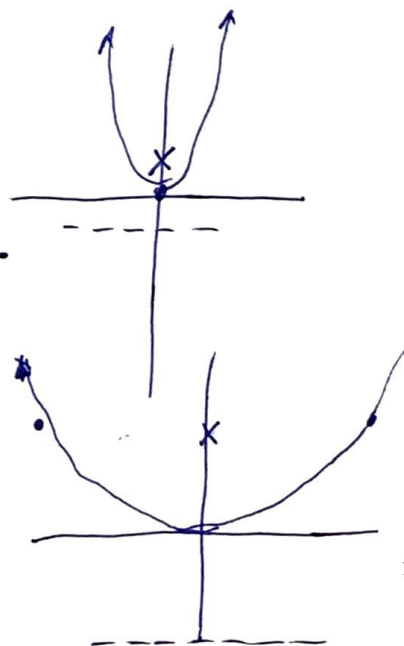
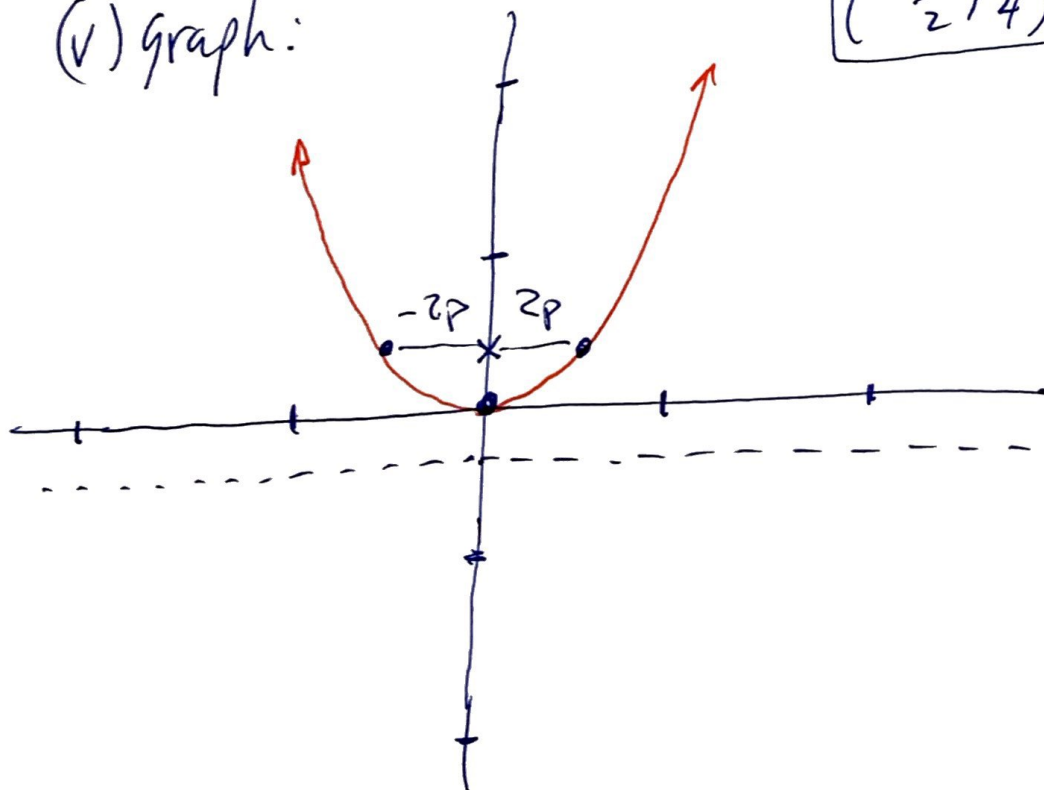
directrix: $y = -\frac{1}{4}$

L.R.-end points: $(-2p, \frac{1}{4})$ & $(+2p, \frac{1}{4})$

$(-\frac{2}{4}, \frac{1}{4})$, $(\frac{2}{4}, \frac{1}{4})$

$(-\frac{1}{2}, \frac{1}{4})$ & $(\frac{1}{2}, \frac{1}{4})$

(v) graph:



[3] Tell me all about $(y-2)^2 = -\frac{4}{5}(x+4)$

(i)