

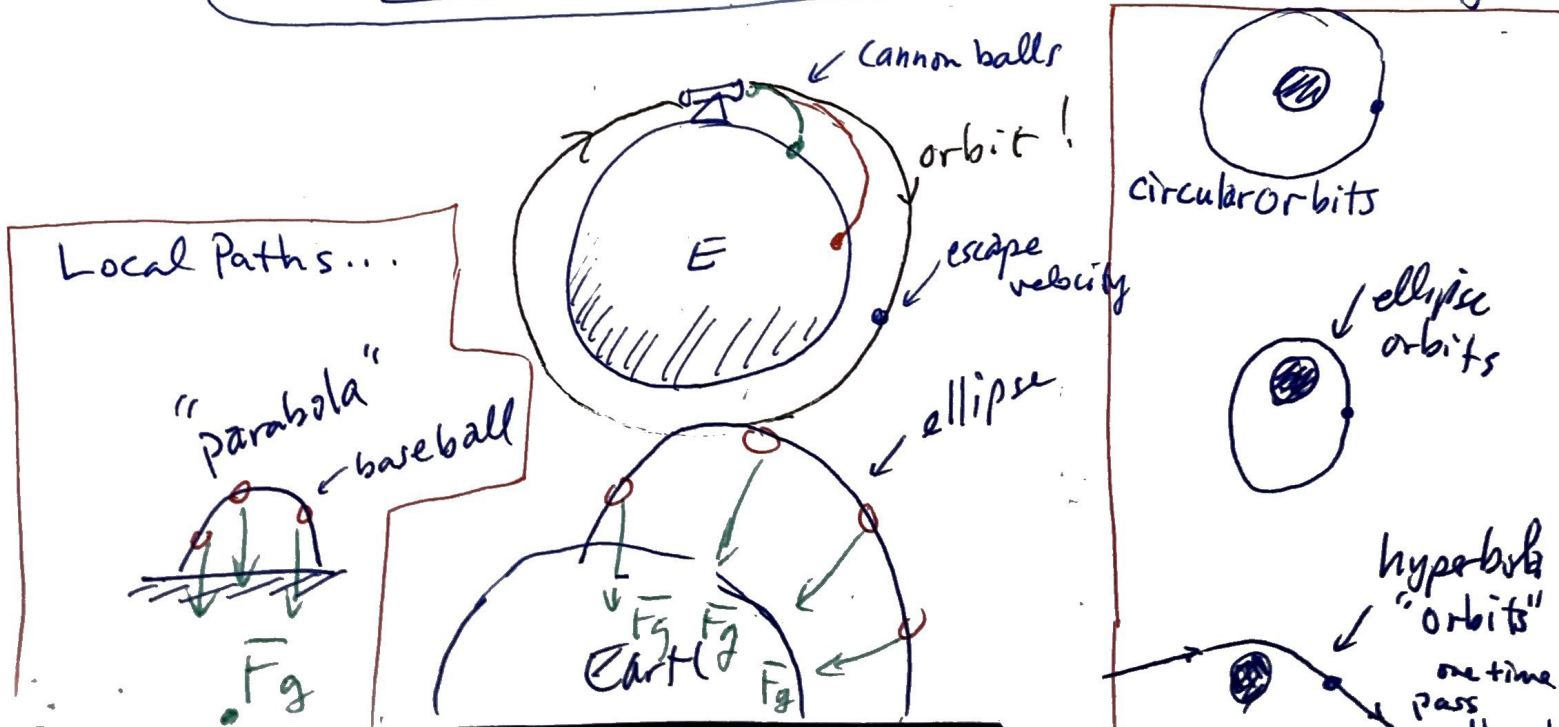
SB

Gravitational Force.

• Newton surmised his First Law ^{the} ^{at a constant speed} ^{in a straight} ^{at a const. s} ^{line unless} one that says "if you are traveling in a straight line, you will continue in a straight line unless you are under the influence of a force".

• But the earth does not travel in a straight line so there must be a force. Like wise, when the apple falls off the tree it acc'd's, it is speeding up, so there must be a force.

• Are these two different forces? Newton observed the moon's orbit and concluded that the force on the apple and on the moon are the same. He called this force - "Gravity".

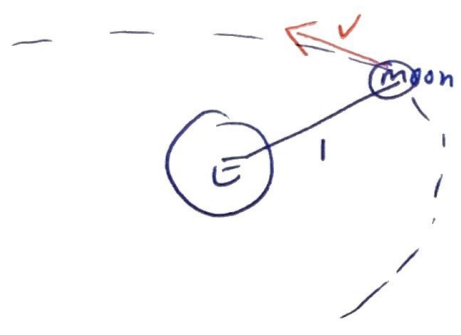


⊗ Newton's 4th LAW: Two masses attract each other - modelled by: (2)



$$F_G = G \frac{M_s m_e}{R_{s.e.}^2}$$

↑ constant of proportionality
 ← mass of object 1
 ← mass of object 2
 ← distance between objects

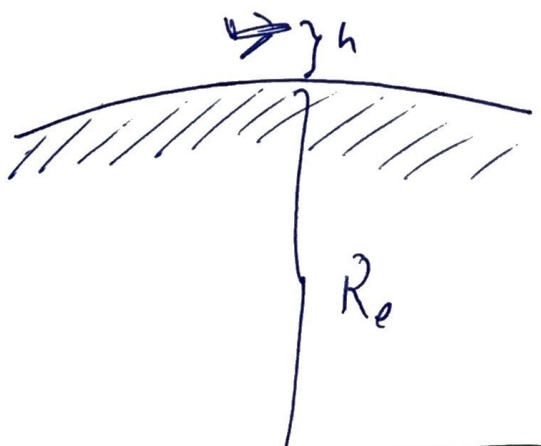


$$F_G = G \frac{M_E m_{moon}}{R_{E.m}^2}$$



$$F_G = G \frac{M_{asteroid} m_{rock}}{R_{A.R.}^2}$$

- Near the surface, the force is calculated using the distance from the center of the Earth.



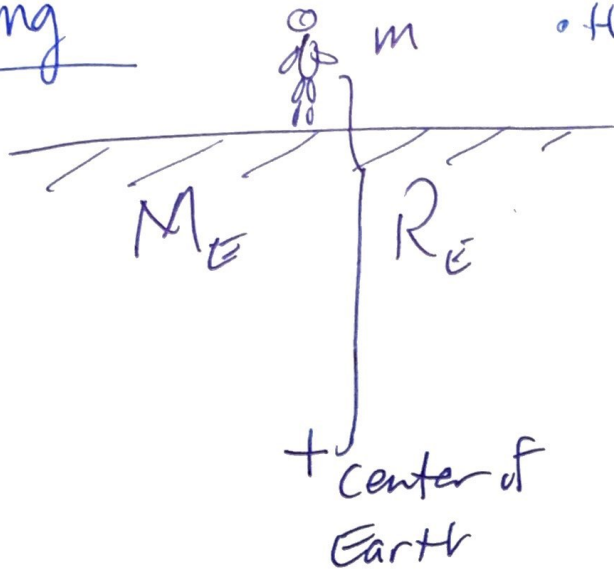
$$F_G = G \frac{M_E m_{airplane}}{(R_e + h)^2}$$

+ In calc. based physics we learn that the net effect of the planes forces of gravity caused by all masses in the Earth has a net effect as an attraction of all mass compressed to the center.

(*) $F = mg$

• Here we derive "g"

(3)



$$F_g = \left(G \frac{M_E}{R_E^2} \right) m$$

Compare to

$$F_g = (g)m$$

So $g = G \frac{M_E}{R_E^2}$

$$G = 6.67 \times 10^{-11} \frac{\text{Nm}^2}{\text{kg}^2}$$

Gravitational Constant.

$$M_E = 5.98 \times 10^{24} \text{ kg}$$

mass of earth

$$R_E = 6.38 \times 10^6 \text{ m}$$

radius of earth

$$\frac{\text{N}}{\text{kg}} = \frac{\cancel{\text{kg}} \text{ m/s}^2}{\cancel{\text{kg}}}$$

• Now

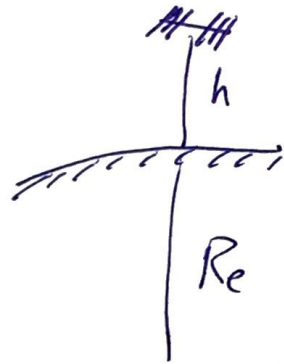
$$g = \frac{\left(6.67 \times 10^{-11} \frac{\text{Nm}^2}{\text{kg}^2} \right) \left(5.98 \times 10^{24} \text{ kg} \right)}{\left(6.38 \times 10^6 \text{ m} \right)^2}$$

or $g = 9.799 \text{ m/s}^2$ or just acceleration due to gravitational attraction →

$$9.8 \text{ m/s}^2$$

Ex The ISS is at 240 km above the Earth. What is "g" up there? (4)

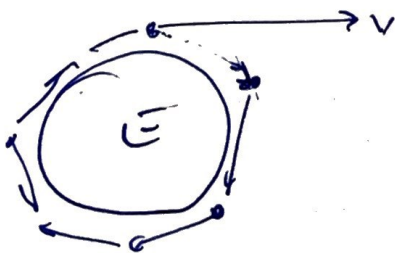
$$g_{ISS} = G \cdot \frac{M_e}{(R_e + 240 \text{ km})^2}$$
$$= \frac{(6.67 \times 10^{-11}) (5.98 \times 10^{24})}{(6.38 \times 10^6 + \underline{\underline{2.4 \times 10^5 \text{ m}}})^2}$$



$$= \boxed{9.10 \text{ m/s}^2}$$

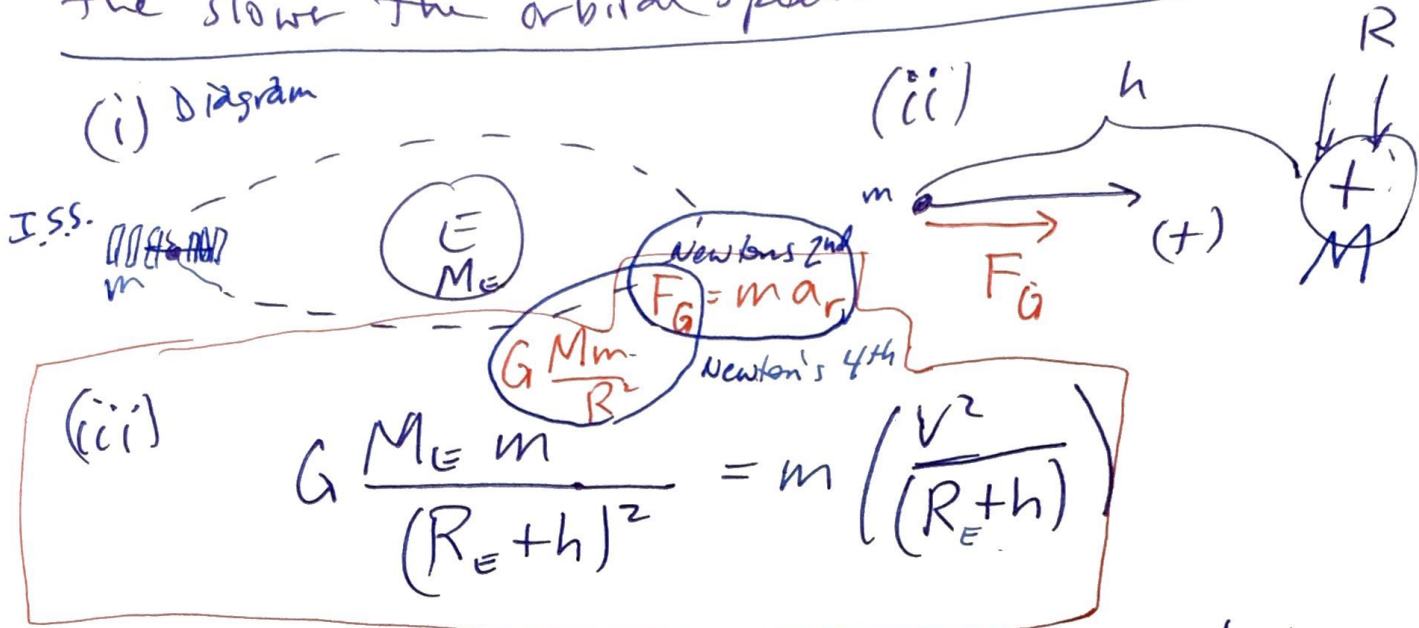
But wait ... the astronauts floats! so is not $g = 0$?

Ans: No the astronauts are falling all the time but the space station is moving so fast that their fall misses the Earth constantly.



⊗ The Further away we get from the Earth (5) the slower the orbital speed. Find v at diff't orbits...

(i) Diagram



(iv) Solve the velocity needed to maintain orbit for $(R_E + h)$.

$$G \frac{M_E m (R_E + h)}{m (R_E + h)^2} = v^2$$

$$v = \sqrt{G M_E / (R_E + h)}$$

Ex How fast is the ISS moving?

$$v = \sqrt{(6.67 \times 10^{-11}) (5.98 \times 10^{24}) / \{6.38 \times 10^6 + 240,000\text{m}\}}$$

$$v = 7762 \text{ m/s} \left(\frac{1 \text{ km}}{1000 \text{ m}} \right) \left(\frac{3600 \text{ s}}{1 \text{ hr}} \right) = 27,943.9 \text{ km/hr.}$$

$$= \boxed{17,363.6 \text{ miles/hr}}$$

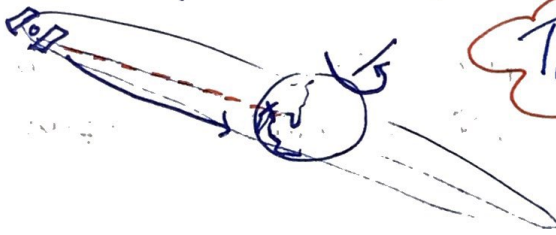
* geo synchronous orbit.

As we orbit further and further from the Earth, the speed decreases:

$$v = \sqrt{GM_E / (R+h)} \text{ as } h \uparrow, v \downarrow$$

There is an orbital distance where the period of orbit matches the period of the Earth. This is called geo synchronous orbit

- Perfect place to park a satellite -



The satellite is above the same spot always.
Dish TV

- Newton's Laws:

$$F_G = m \frac{v^2}{R+h}$$

$$G \frac{M_e m}{(R+h)^2} = m \frac{v^2}{R+h}$$

$$\frac{GM_e}{v^2} = R+h$$

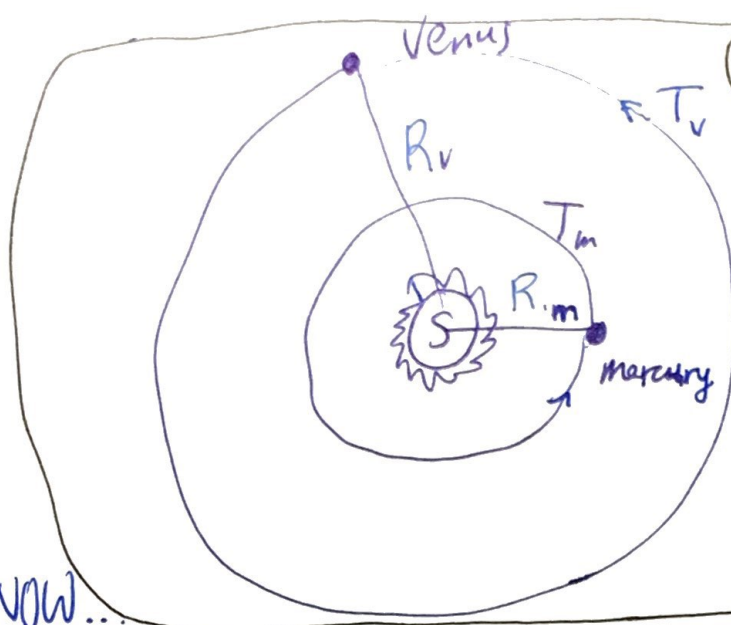
$$\frac{GM}{\left[\frac{2\pi(R+h)}{T}\right]^2} = R+h$$

$$\left(\frac{GM}{4\pi^2}\right) T^2 = (R+h)^3$$

period squared = Radius Cubed

but
$$v = \frac{\text{Circumference}}{\text{Period}} = \frac{2\pi(R+h)}{24\text{hr}}$$

"Kepler's Law"



Applied To Planets

$$\begin{aligned}
 h_m^3 &\propto T_m^2 \\
 h_v^3 &\propto T_v^2 \\
 &\vdots \\
 &\boxed{T \propto h^{3/2}}
 \end{aligned}
 \quad
 \left(\frac{h_m}{h_v} \right)^3 = \left(\frac{T_m}{T_v} \right)^2$$

EX

NOW...

- Solve for "R+h" that keeps a satellite above Calif:
 - Kepler's Law

$$R+h = \sqrt[3]{G \frac{M T^2}{4\pi^2}}$$

↑ earth ↑ we want 24hr.

$$\sqrt[3]{a} = a^{1/3}$$

- Populate

$$R+h = \left(\frac{6.67 \times 10^{-11} (5.98 \times 10^{24}) (24 \text{ hr} \cdot \frac{3600 \text{ s}}{\text{hr}})^2}{4\pi^2} \right)^{1/3}$$

$$= (7.54 \times 10^{22} \text{ m}^3)^{1/3}$$

$$= \boxed{4.23 \times 10^7 \text{ m}} = R+h$$

↑ center of earth to geo. satellite

$$= 4.23 \times 10^4 \text{ km} = \boxed{42,300 \text{ km}}$$

from center of the Earth

(*) Gravity is one of the 4 forces in Nature. (8)

The others are

- ElectroMagnetic - pos & neg charges attract {static electricity}, North and South Poles on magnets attract.
- Weak force - force between sub-atomic particles
- Strong force - force between protons and neutrons. Keeps atoms together.