

Try to keep your work on these sheets if possible. Show or explain ALL work for full credit. Staple extra work, if needed, done on white paper, after the page of the test possessing the problem. All problems, or parts therein, are 5 pts unless otherwise noted.

1. (10 pts) Determine whether the relation is a function, and if so, is it a 1-to-1 function? Give a brief statement of support for your conclusion(s).

(a) Table: { (a, b), (c, d), (e, d) }

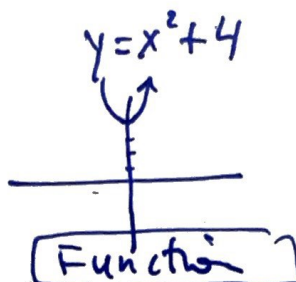
x	y
a	b
c	d
e	d

function: only one output for each input

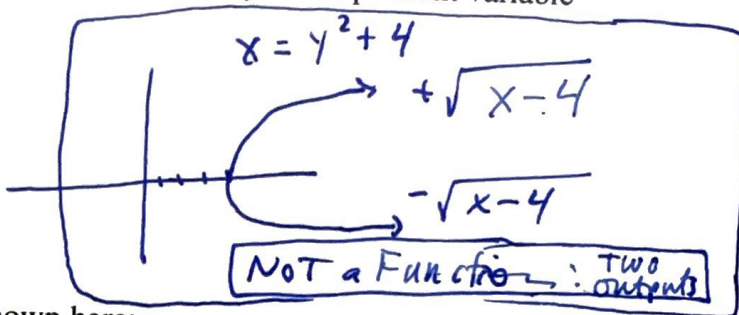
NOT 1-1: "c" and "e" both have the same output

3

(b) Analytical: $y^2 + 4 = x$, for x the independent variable and y the dependent variable

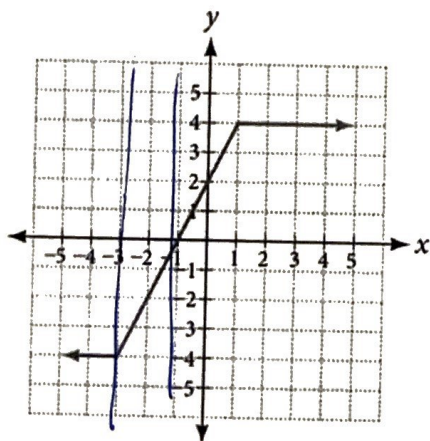


swap
→
x for
y



4

(c) Graphical: the relation whose graph is shown here:



Function: yes (vert. Line Test)
Not 1-1: Fails Horiz. Test

3

Note: No point in addressing 1-to-1 if a relation is not a function.

2. (10 pts) Construct $\frac{f(x+h)-f(x)}{h}$ for $f(x) = -2x^3+3x+2$

$$= \frac{[-2(x+h)^3 + 3(x+h) + 2] - [-2x^3 + 3x + 2]}{h}$$

$$= \frac{[-2(x^3 + 3x^2h + 3xh^2 + h^3) + 3x + 3h + 2] + 2x^3 - 3x - 2}{h}$$

$$= \frac{-2x^3 - 6x^2h - 6xh^2 - 2h^3 + 3x + 3h + 2 + 2x^3 - 3x - 2}{h}$$

$$= \frac{-6x^2h - 6xh^2 - 2h^3 + 3h}{h}$$

$$= \boxed{-6x^2 + 3 - 6xh - 2h^2}$$

as $h \rightarrow 0$ then $\frac{\Delta f}{\Delta x} \rightarrow -6x^2 + 3$; the derivative of $f(x)$

3. (5 pts) Express the domain of the function using interval notation: $f(x) = \frac{\sqrt{x-4}}{\sqrt{x-6}}$

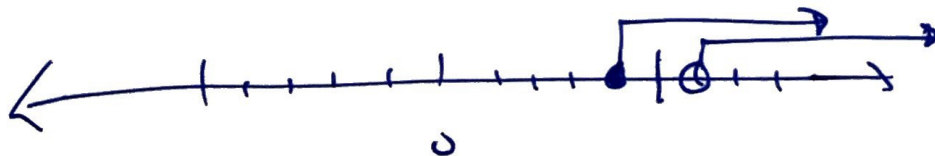
$$\sqrt{x-6} \neq 0 \quad \text{so} \quad \boxed{x \neq 6}$$

$$x-6 > 0 \quad \text{so} \quad \boxed{x > 6}$$

But $x-4 \geq 0$ also

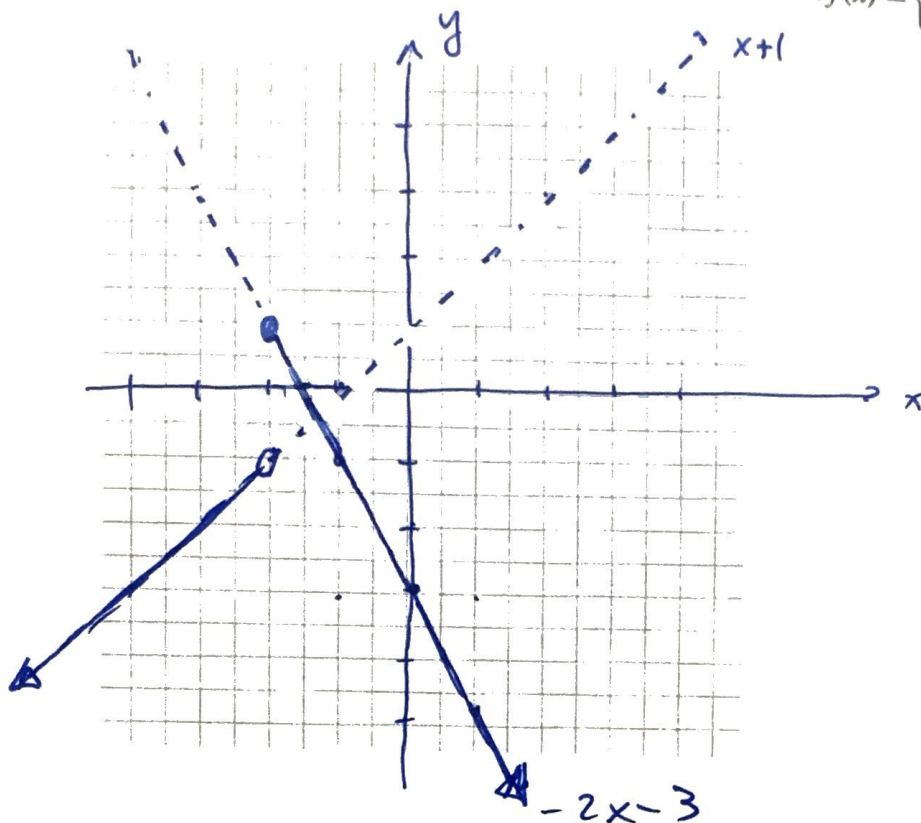
$$\text{so} \quad \boxed{x \geq 4}$$

$$\boxed{D_f : \{x \mid x > 6\}}$$



4. (5 pts) Graph this piecewise function

$$f(x) = \begin{cases} x+1 & x < -2 \\ -2x-3 & x \geq -2 \end{cases}$$



5. (5 pts) Find the average rate of change of the function $f(x) = 5x^3 + 4$ from $x = 1$ to $x = 2$

$$\frac{\Delta f}{\Delta x}$$

from $x = 1$ to 2

$$= \frac{f(2) - f(1)}{2 - 1}$$

$$= \frac{[5(2)^3 + 4] - [5(1)^3 + 4]}{1}$$

$$= \frac{5 \cdot 8 + 4 - 5 - 4}{1}$$

$$= \frac{44 - 9}{1} = \boxed{35}$$

6. (5 pts) Solve for x , naming all steps along the way. Keep the $=$ sign lines up down the page.

$$2(3x - 7) + 3(x + 1) + x = 2x - 5 - (6 - 2x) + 11$$

$$6x - 14 + 3x + 3 + x = 2x - 5 - 6 + 2x + 11$$

$$10x - 11 = 4x + 0$$

$$10x - 4x = 0 + 11$$

$$6x = 11$$

$$x = \frac{11}{6}$$

Distribute

Simplify

gather

Simplify

isolate x

5

7. (5 pts) Simplify the relation: $\left(\frac{x^{-5}y^5z^{-3}}{xyx}\right)^{-3/5}$ so that the final answer has no negative exponents.

$$= \left(x^{-5-1-1} y^{5-1} z^{-3}\right)^{-3/5}$$

$$= \left(x^{-7} y^4 z^{-3}\right)^{-3/5}$$

$$= \sqrt[5]{\frac{y^4}{z^7 z^3}}$$

$$= x^{-7 \cdot (-3/5)} y^{4 \cdot (-3/5)} z^{-3 \cdot (-3/5)}$$

$$= x^{21/5} y^{-12/5} z^{9/5}$$

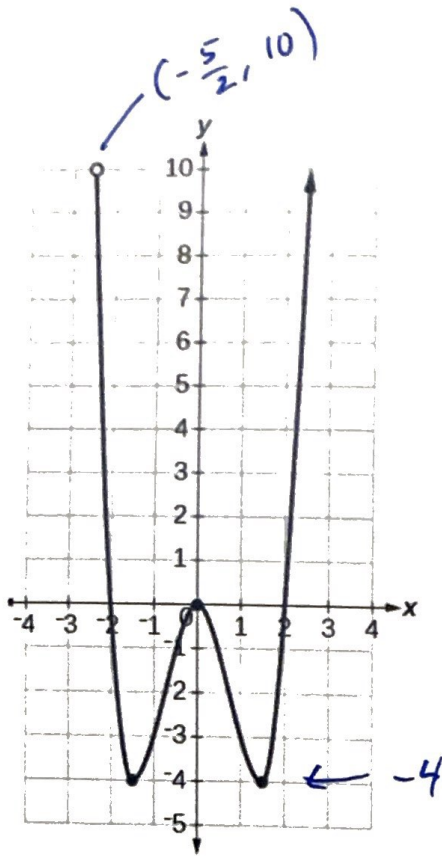
$$= \frac{x^{21/5} z^{9/5}}{y^{12/5}} \quad \text{or} \quad \sqrt[5]{\frac{x^{21} z^9}{y^{12}}}$$

10

8. (10 pts) State the Domain and Range, in set builder notation, for the graphs. Approximate to the nearest 1/2 unit.

5

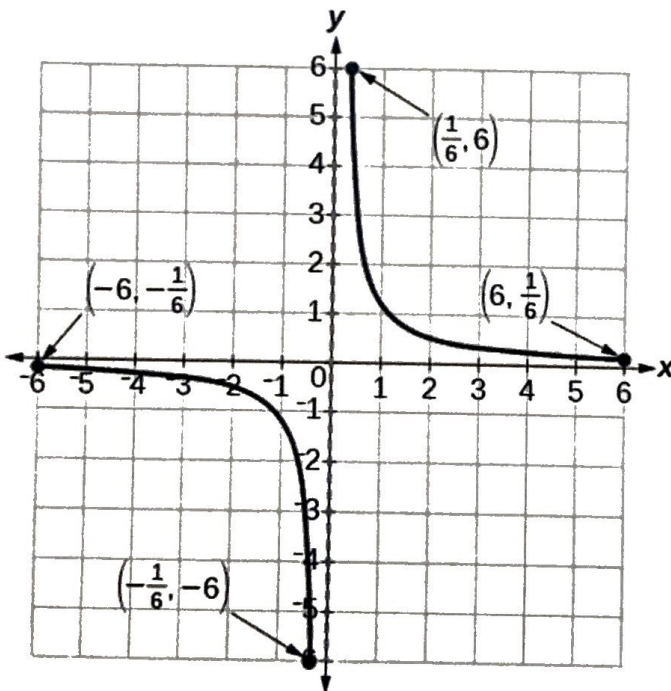
(a)



Domain: $\{x \mid x > -\frac{5}{2}\}$

Range: $\{y \mid y \geq -4\}$

(b)



Domain: $\{x \mid x \in (-6, -\frac{1}{6}) \cup (\frac{1}{6}, 6)\}$

Range: $\{y \mid y \in (-6, -\frac{1}{6}) \cup (\frac{1}{6}, 6)\}$

5

10